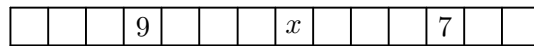


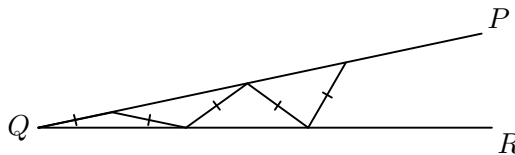
1. The value of  $\frac{1001^2 - 999^2}{101^2 - 99^2}$  is  
 (A) 1            (B) 10            (C) 20            (D) 40            (E) 100
2. Let  $S$  be the set of three-digit numbers where all the digits are equal to 1 or 2. Find the sum of all numbers in  $S$ .  
 (A) 1332            (B) 333            (C) 999            (D) 666            (E) 1665
3. How many of the following numbers are greater than 10?

$$3\sqrt{11}, \quad 4\sqrt{7}, \quad 5\sqrt{5}, \quad 6\sqrt{3}, \quad 7\sqrt{2}.$$

- (A) 1            (B) 3            (C) 5            (D) 4            (E) 2
4. The 14 digits of a credit card are to be written in the boxes below. If the sum of any three consecutive digits is 20, then the value of  $x$  is



- (A) 3            (B) 4            (C) 5            (D) 7            (E) 9
5. In the diagram below,  $\angle PQR = 12^\circ$ , and a sequence of isosceles triangles is drawn as shown.



- What is the largest number of isosceles triangles that can be drawn?  
 (A) 8            (B) 4            (C) 5            (D) 7            (E) 6
6. The numbers  $a, b, c, d,$  and  $e$  are equal to the numbers 1, 2, 3, 4, and 5 in some order. The largest possible value of  $ab + bc + cd + de$  is  
 (A) 40            (B) 43            (C) 45            (D) 46            (E) 49
7. If  $x^2 = 3x + 1$ , then  $x^3$  is equal to  
 (A)  $10x + 3$             (B)  $4x + 1$             (C)  $4x + 3$             (D)  $13x + 3$             (E)  $10x + 1$
8. Two numbers  $x$  and  $y$  satisfy three of the following equations but not the remaining equation. What is the value of  $x$ ?

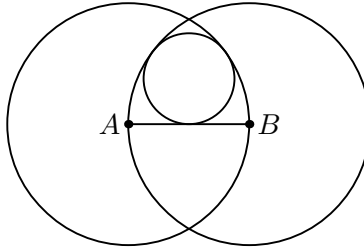
$$x + y = 63, \quad x - y = 47, \quad xy = 392, \quad x/y = 8.$$

- (A) 7            (B) 8            (C)  $\frac{196}{3}$             (D) 55            (E) 56

9. If  $a$  and  $b$  are real numbers such that  $0 < a < b$  and  $a^2 + b^2 = 6ab$ , then  $\frac{a+b}{a-b}$  is equal to

- (A)  $\sqrt{2}$       (B)  $2\sqrt{2}$       (C)  $2\sqrt{2}$       (D)  $-\sqrt{2}$       (E)  $\sqrt{6}$

10. The distance between the points  $A$  and  $B$  is 2. The circle with center  $A$  and radius 2 is drawn, as well as the circle with center  $B$  and radius 2. A third circle is drawn that is tangent to both circles, and segment  $\overline{AB}$ , as shown below. Find the area of this third circle.

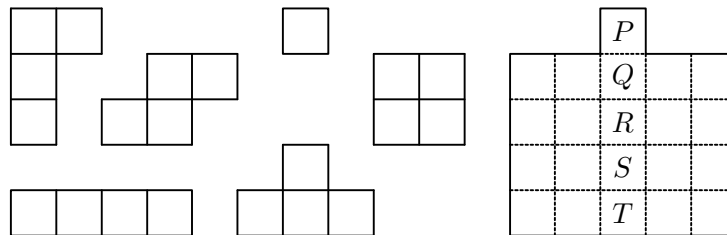


- (A)  $\frac{9\pi}{16}$       (B)  $\frac{3}{4}$       (C)  $\frac{5\pi}{8}$       (D)  $\frac{3}{8}$       (E)  $\frac{7\pi}{8}$

11. If  $x = \sec \theta + \tan \theta$  and  $y = \sec \theta - \tan \theta$ , then which of the following is true for all values of  $\theta$  for which  $x$  and  $y$  are defined?

- (A)  $x + y = 2$       (B)  $xy = 1$       (C)  $x^2 + y^2 = 2$   
(D)  $x^2 + y^2 = 1$       (E)  $x - y = 2$

12. The six tiles on the left can be re-arranged to completely cover the shape on the right, without overlap. The tiles may be rotated and/or reflected. Which square must the tile consisting of one unit square cover?



- (A)  $P$       (B)  $Q$       (C)  $R$       (D)  $S$       (E)  $T$

13. When the expression

$$(x_1 + x_2 + x_3 + x_4 + \cdots + x_9 + x_{10})(x_1 - x_2 + x_3 - x_4 + \cdots + x_9 - x_{10})$$

is expanded and simplified, how many different terms appear?

- (A) 20      (B) 25      (C) 30      (D) 35      (E) 50

14. The least common multiple of  $10! \cdot 18!$  and  $12! \cdot 17!$  is

- (A)  $\frac{18! \cdot 12!}{6!}$       (B)  $18! \cdot 17!$       (C)  $\frac{12! \cdot 18!}{3!}$       (D)  $12! \cdot 18!$       (E)  $\frac{18! \cdot 17!}{6!}$

15. When the product  $1 \cdot 3 \times 5 \times 7 \cdots 99$  is written as a number, its tens digit is

- (A) 2      (B) 7      (C) 5      (D) 0      (E) 3